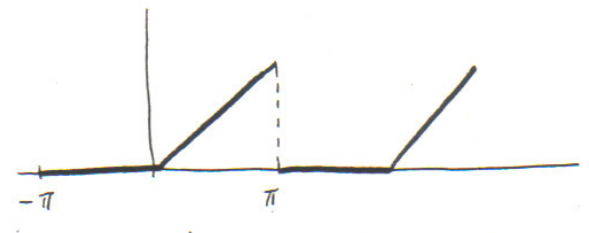


7-5,7

$$f(x) = 0 \quad -\pi < x \leq 0$$

$$f(x) = x \quad 0 \leq x < \pi$$

$$2l = 2\pi$$



$$a_0 = \frac{1}{\pi} \int_0^{2\pi} f(x) dx = \frac{1}{\pi} \left[\int_{-\pi}^{\pi} f(x) dx + \int_0^{\pi} f(x) dx \right]$$

$$a_0 = 0 + \frac{1}{\pi} \int_0^{\pi} x dx = \frac{1}{\pi} \left[\frac{1}{2} x^2 \right]_0^{\pi}$$

$$a_0 = \frac{1}{2\pi} (\pi^2 - 0) = \frac{\pi}{2}$$

$$a_n = \frac{1}{\pi} \int_0^{\pi} x \cos nx dx = \frac{1}{\pi} \left[\frac{1}{n^2} \cos nx + \frac{x}{n} \sin nx \right]_0^{\pi}$$

$$= \frac{1}{\pi} \left[\left(\frac{1}{n^2} \cos n\pi + \frac{\pi}{n} \sin n\pi \right) - \left(\frac{1}{n^2} \cos n \cdot 0 + 0 \right) \right] = \frac{1}{\pi} \left[\frac{1}{n^2} (\cos n\pi - 1) \right]$$

$$= \frac{1}{\pi} \left[\frac{1}{n^2} \begin{matrix} \text{even} \\ \pm 1 \end{matrix} + 0 \right] - \left(\frac{1}{n^2} \right) = \frac{1}{\pi n^2} [\pm 1 - 1]$$

$a_n = \frac{-1}{\pi n^2}$ for n odd	e.g. $-\frac{2}{\pi}$, $-\frac{2}{9\pi}$, $-\frac{2}{25\pi}$ etc.
$a_n = 0$ for n even	

$$b_n = \frac{1}{\pi} \int_0^{\pi} x \sin nx dx = \frac{1}{\pi} \left[\frac{1}{n^2} (\sin nx) - \frac{x}{n} \cos nx \right]_0^{\pi}$$

$$= \frac{1}{\pi} \left[\frac{1}{n^2} (\sin n\pi) - \frac{\pi}{n} \cos n\pi - 0 + 0 \right] = -\frac{1}{n} \cos n\pi$$

$$b_n = \pm \frac{1}{n} \left\{ \begin{matrix} n \text{ even} \\ n \text{ odd} \end{matrix} \right\} \frac{1}{n} (-1)^{n+1}$$

Hence

$$f(x) = \frac{\pi}{4} - \frac{2}{\pi} \left(\cos x + \frac{\cos 3x}{9} + \frac{\cos 5x}{25} + \dots \right) + \left(\sin x - \frac{\sin 2x}{2} + \frac{\sin 3x}{3} - \frac{\sin 4x}{4} + \dots \right)$$

$$f(x) = \frac{\pi}{4} - \frac{2}{\pi} \sum_{n=1}^{\infty} \frac{\cos((2n-1)x)}{(2n-1)^2} + \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n} \sin nx$$