

2-5.32 Using  $|z| = \sqrt{z\bar{z}}$ , we have

$$\begin{aligned} |(2-3i)^4| &= \sqrt{(2-3i)^4(2+3i)^4} = \sqrt{[(2-3i)(2+3i)]^4} \\ &= \sqrt{(2^2+3^2)^4} = \sqrt{13^4} = 13^2 = 169. \end{aligned}$$

2-5.43.

Given  $(x+iy)^2 = 2ix$ , we multiply out the left side to get

$$x^2 - y^2 + 2ixy = 2ix = 0 + 2ix.$$

Equating real terms and equating imaginary terms gives

$$x^2 - y^2 = 0 \quad \text{and} \quad 2xy = 2x.$$

The second equation is true if  $x=0$  or if  $y=1$ . If  $x=0$ , then  $y=0$  by the first equation. If  $y=1$ , then  $x=\pm 1$  from the first equation. Thus there are three points satisfying the given equation:  $(x,y) = (0,0)$  or  $(1,1)$  or  $(-1,1)$ .