#### MAT 095 and 096 courses do not count toward graduation requirements.

#### MAT 095/Intermediate Algebra

(every semester) Prerequisites: See

http://www.tcnj.edu/~mathstat/calcrec.html for details

This course is designed for students majoring in a field where at least one of the courses, Pre-Calculus (MAT 096), Calculus A (MAT 127), or Calculus for Business and the Social Sciences (MAT 125) is required. Conceptual understanding and skill development of traditional algebraic topics such as: linear equations and inequalities, exponents and polynomials, rational expressions, quadratic equations, and systems of linear equations are included.

#### MAT 096/Pre-Calculus

(every semester) *Prerequisite:* MAT 095 or placement into MAT 096 See <u>http://www.tcnj.edu/~mathstat/calcrec.html</u> for details

This course is only for students going on to calculus. Fundamentals of algebra, trigonometry, and analytic geometry. Stress is on computational and problem-solving techniques.

#### MAT 099/Orientation to Mathematics and Statistics

(seven weeks)

(fall)

Required as an entry course of all entering first year students enrolled in majors offered by the Department of Mathematics and Statistics. Topics covered include degree requirements, general information about the college and services offered, career opportunities in mathematics and statistics, academic standards and integrity, study habits and time management, and resume development. General and personal advisement relative to pursuit of the major and the degree is also included.

#### MAT 101/Applied Liberal Arts Mathematics

(every semester)

Provides intuitive and formal experience in development and appreciation of structural bases characteristic of mathematics. Topics from: logic, sets, graph theory, coding, voting, and social choice and game theory.

#### MAT 102/Mathematics for the Liberal Arts

(spring)

Provides intuitive and formal experience in development and appreciation of structural base characteristics of mathematics. Topics from: logic, sets, combinatorial probability, abstract mathematical systems, and number theory.

# MAT 105/Mathematical Structures and Algorithms for Educators I 1 course unit (every semester)

*Prerequisite*: Reserved for School of Education students

This course concerns the development of number systems, algebraic structures, and algorithms. The student will be required to reason mathematically, solve problems, and communicate mathematics effectively at different levels of formality, using a variety of representations of mathematical concepts and procedures. Physical materials and models will be used to explore fundamental properties of number systems, to model algorithms, and to explore selected algebraic structures. This course is especially appropriate for those students preparing to be elementary, early childhood, deaf and hard of hearing, or special education teachers.

# MAT 106/Mathematical Structures and Algorithms for Educators II 1 course unit (every semester)

*Prerequisite*: Reserved for school of education students

Physical materials and models will be used to explore fundamental concepts of geometry, measurement, data analysis, statistics, and probability. The student will be required to reason mathematically, solve problems, and communicate mathematics effectively at different levels of

additive credit

C ( 11

1 course unit

# 0 course units

additive credit

formality, using a variety of representations of mathematical concepts and procedures. This course is especially appropriate for those students preparing to be elementary, early childhood, deaf and hard of hearing, or special education teachers.

#### MAT 111/Number Theory and Systems for Middle School Teachers 1 course unit (every semester)

Prerequisite: MAT 105 or MAT 106

This course gives the middle school mathematics teacher a deeper understanding of numbers and operations. Physical materials, models, technology, and middle school curricula will be used to explore these topics. Exploration of ways to engage middle school students meaningfully in experiences that lay a strong foundation for more formal work in number theory will be integrated with the mathematics content.

#### MAT 112/Data Analysis and Problems for Middle School Teachers 1 course unit (every semester)

*Prerequisite*: MAT 105 or MAT 106

This course gives the middle school mathematics teacher a deeper understanding of data analysis and probability. Physical materials, models, technology, and middle school curricula will be used to explore these topics. Exploration of ways to engage middle school students meaningfully in experiences that lay a strong foundation for more formal work in data analysis and probability will be integrated with the mathematics content.

#### MAT 114/Patterns, Functions and Algorithms for Middle School Teachers 1 course unit (every semester)

Prerequisite: MAT 105 or MAT 106

This course gives the middle school mathematics teacher a deeper understanding of patterns, functions, and algebra. Physical materials, models, technology, and middle school curricula will be used to explore these topics. Exploration of ways to engage middle school students meaningfully in experiences that lay a strong foundation for more formal algebraic work will be integrated with the mathematics content.

## MAT 115/Geometry for Middle School Teachers

(every semester)

Prerequisite: MAT 105 or MAT 106

This course gives the middle school mathematics teacher a deeper understanding of geometry. Physical materials, models, technology, and middle school curricula will be used to explore these topics. Exploration of ways to engage middle school students meaningfully in experiences that lay a strong foundation for more formal work in geometry will be integrated with the mathematics content.

#### MAT 117/Discrete Math for Middle School Teachers

(every semester)

#### Prereauisite: MAT 105 or MAT 106

This course gives the middle school mathematics teacher a deeper understanding of discrete mathematics. Physical materials, models, technology, and middle school curricula will be used to explore these topics. Exploration of ways to engage middle school students meaningfully in experiences that lay a strong foundation for more formal work in discrete math will be integrated with the mathematics content.

#### MAT 118/Concepts of Calculus for Middle School Teachers

(every semester)

#### Prerequisite: MAT 105 or MAT 106

This course gives the middle school mathematics teacher a deeper understanding of mathematics through the study of calculus. Physical materials, models, technology, and middle school curricula will be used to explore the topics. Exploration of ways to engage middle school students meaningfully in experiences that lay a strong foundation of the ideas of calculus will be integrated with the mathematics content.

1 course unit

1 course unit

### MAT 125/Calculus for Business and the Social Sciences

(every semester) Prerequisite: MAT 096 or an SAT math score at least 650 See http://www.tcnj.edu/~mathstat/calcrec.html for details

A course intended for majors in business and the social sciences, and/or minors in statistics. Topics include differential calculus, integral calculus, and some linear algebra, with applications to areas of business and social science. Not for mathematics or science majors.

### MAT 127/Calculus A

(every semester)

Prerequisite: MAT 096 or an SAT math score at least 650 See http://www.tcnj.edu/~mathstat/calcrec.html for details

Provides students with a solid grounding in single-variable calculus. The course is designed for students in the mathematical and physical sciences. Topics include functions and limits, derivatives and differentiation rules, applications of derivatives, and an introduction to integrals and their applications.

### MAT 128/Calculus B

(every semester) *Prerequisite*: MAT 125 or 127

A second course in calculus covering integral calculus and series. The course will cover both the theoretical and applied aspects of calculus.

### **MAT 170/Topics in Mathematics**

(occasionally)

### MAT 200/Proof Writing through Discrete Mathematics

(every semester)

*Prerequisite:* MAT 096 or an SAT math score >=650

An introduction to discrete mathematics. Discrete topics include sets, graphs, Euler and Hamilton circuits, connectivity, planar graphs, recursion and difference equations. Descriptions of the proof types such as direct, indirect, cases, contrapositive and induction should be worked into the material whenever possible. Some optional topics should be included such as fractals, algorithms, combinatorial proofs, discrete codes, logic, Platonic solids and combinatorial counting.

### MAT 205/Linear Algebra: Theory and Applications

(every semester) (Writing Intensive)

Prerequisite: MAT 128 or MAT 200 or CSC 310

An introduction to vector spaces and systems of linear equations essential for the understanding of both pure and applied mathematics. Selected topics include: systems of linear equations, matrices, linear transformations, linear independence, determinants, vector spaces, eigenvalues and eigenvectors, and orthogonality.

### MAT 229/Multivariable Calculus

(every semester)

Prerequisite: MAT 128

Topics include: geometry of three dimensional space, derivatives of functions of several variables, integrals in dimension two and three, and Stoke's theorem.

### MAT 255/Perspectives on the Development of Mathematics

(every semester)

*Prerequisite*: Reserved for math students

The course develops a skeletal outline of the history of mathematics. Additional topics may include the history of a specific area of mathematics. Samples of topics that may be covered in the course are: ancient mathematics, the relation between Greek and Mesopotamian algebra, the growth of trigonometric ideas, the geometric solution of the cubic equations by Omar Khayyam

### 1 course unit

1 course unit

### 1 course unit

1 course unit

### 1 course unit

#### 1 course unit

#### 1 course unit

and the algebraic solutions by Cardano, Zeno's paradox and the development of different number systems.

#### MAT 270/Topics in Mathematics

(occasionally) Special topics in mathematics that will vary by semester.

#### MAT 301/Number Theory

(every semester) Prerequisite: MAT 200

Divisibility, primes, unique factorization, diophantine equations, congruences, quadratic reciprocity, and such optional topics as sums of squares, number-theoretic functions, continued fractions, prime number theory, public-key encryption, and elliptic curves.

#### MAT 305/Abstract Algebra

(every semester)

Prerequisites: MAT 200 and MAT 205

An introduction to groups, rings, integral domains and fields. Additional topics include groups of symmetries, rings of integers, rings of polynomials and construction of the field of rational numbers.

#### MAT 310/Real Analysis

(every semester)

Prerequisites: MAT 200 and MAT 229

A logical development of mathematical analysis for functions of a single real variable. Topics include order, completeness, sequences, series, limits of functions, basic topology of the reals, differentiation, integration, sequences and series of functions and transcendental functions.

#### MAT 315/Topics in Linear Algebra

(periodically)

Prerequisite: MAT 205

The course consists of a collection of topics not covered in MAT 205 but built upon the material covered in MAT 205. Such topics may include: the Spectral Theorem of Symmetric Matrices, Quadratic Forms, Unitary and Hermitian Matrices, Jordan Canonical Forms, Schur's Theorem, applications to Linear Programming and Markov chains.

#### MAT 316/Probability

(every semester)

Prerequisites: MAT 200 and MAT 229

Topics will include counting rules to derive models for discrete variables, including the uniform, Bernoulli, binomial, geometric, negative binomial, hypergeometric and Poisson distributions. Continuous variables will be modeled with distributions having a variety of shapes, including the uniform, exponential, gamma, beta and normal distributions.

#### **MAT 318/Mathematical Statistics**

(fall)

Prerequisites: STA 215 and MAT 316

Topics include: theory of sampling, law of large numbers, central limit theorem, normal approximation to binomial and poisson distributions, estimation of population parameters. hypothesis testing, confidence methods, change of variable and order statistics.

#### MAT 320/Complex Analysis

(spring)

Prerequisite: MAT 229

A logical development of the classical theory of functions of a complex variable, with emphasis on those parts of the theory which are most used in modern applications of the subject. Topics include: complex numbers, analytic functions, the exponential, trigonometric, hyperbolic, and logarithmic functions and their inverses; mapping by elementary functions; integrals; the

1 course unit

1 course unit

1 course unit

#### 1 course unit

#### 1 course unit

### 1 course unit

1 course unit

Cauchy-Goursat theorem, the Cauchy integral formula, derivatives of analytic functions; the fundamental theorem of algebra; power series; residues and poles; and isolated, essential, and removable singularities.

### **MAT 326/Differential Equations**

(every semester) Prerequisite: MAT 229

Presentation of subject through logical and orderly approach with emphasis on general concepts rather than isolated details. Topics: first-order ordinary differential equations, linear differential equations with constant coefficients, simultaneous differential equations, hyperbolic functions, and Laplace Transforms.

### MAT 331/Numerical Methods

(periodically)

Prerequisites: MAT 128 and MAT 205

Numerical Methods is a course which focuses on methods of approximating solutions to problems for which the techniques of the earlier Calculus courses fail. A course covering methods of approximation, errors in approximation, and efficiency of algorithms.

### MAT 351/Geometry

(every semester)

Prerequisites: MAT 200 and MAT 229

Both Euclidean and non-Euclidean geometries are studied. Each geometry will be understood from three different perspectives: first, as the collection of theorems following from a particular set of axioms; second, as the two-dimensional geometry arising from a particular metric; and third, as the geometry obtained from a set together with a specific group of rigid motions of the set. At least one of these viewpoints will be developed in detail.

MAT 370/Topics in Mathematics (occasionally) Special topics in mathematics that will vary by semester.	1 course unit
MAT 391/Independent Study in Mathematics	variable course units
MAT 392/Guided Study in Mathematics	variable course units
MAT 393/Independent Research in Mathematics (every semester) <i>Prerequisite:</i> By invitation only Student will study and/or do research independently in an appropriate area member will be assigned to advise and direct the student.	variable course units . A department
MAT 399/Internship in Mathematics (every semester) <i>Prerequisites:</i> Junior standing and permission of the department. Applied experience in major field of study. Consult department for details	variable course units
MAT 403/Advanced Calculus	1 course unit

(periodically)

Prerequisite: MAT 229

The calculus of several variables is explored from the point of view of the geometry of surfaces in Euclidean space. The emphasis will be on examples rather than proofs. Topics will include the topology of Euclidean Space, the derivative as a linear map, the geometry of maps whose derivative have maximal rank, and Lie groups such as SL(2,R)

## 1 course unit

#### 1 course unit

### MAT 405/Topology

(periodically)

Prerequisite: MAT 305

Students will gain acquaintance of various aspects of topology and its connections to analysis and algebra. This will include a thorough treatment of those aspects of point-set topology that lay the foundation for graduate study; i.e., continuity, compactness, connectedness and separation axioms. Also, this course will introduce students to manifold theory, including the classification of two-dimensional manifolds. The student will understand the role of topological invariants in the classifying topological spaces. This will lead to the classification of the surfaces. Lastly, students will see categorical relationships between topological objects and algebraic objects.

#### **MAT 407/Projective Geometry**

(occasionally)

*Prerequisite:* MAT 305

An introduction to projective geometry. Topics include affine and projective plane, real projective plane, principle of duality, groups of automorphisms, and projective planes over division rings.

### MAT 440/Mathematical Logic

(occasionally)

Prerequisites: MAT 200, a 300-level MAT course and reserved for juniors and seniors The process, characteristics, and limits of logical reasoning. Several logical languages will be developed from first principles. Students will become familiar with theorems on consistency and independence and develop an appreciation of Godel's incompleteness theorem. An introduction to set theory will be included to discuss infinite cardinals.

#### MAT 451/Seminar in Algebra

(occasionally)

Prerequisites: MAT 229 and MAT 305

A flexible course in which the content is selected from topics in algebra. This is an elective course designed to enrich the background of the student as well as to bridge the gap between undergraduate math and graduate math.

### MAT 452/Seminar in Geometry and Topology

(occasionally)

Prerequisites: MAT 229 and MAT 305

A flexible course in which the content is selected from topics in geometry and topology. This is an elective course designed to enrich the background of the student as well as to bridge the gap between undergraduate math and graduate math.

### MAT 453/Seminar in Analysis

(occasionally)

Prerequisites: MAT 229 and MAT 310

A flexible course in which the content is selected from topics in analysis. This is an elective course designed to enrich the background of the student as well as to bridge the gap between undergraduate math and graduate math.

#### MAT 454/Seminar in Applied Mathematics

(occasionally)

*Prerequisites*: MAT 229 A flexible course in which the content is selected from topics in applied mathematics. This is an elective course designed to enrich the background of the students as well as to bridge the gap between undergraduate math and graduate math.

#### 1 course unit

# 1 course unit

1 course unit

#### 1 course unit

## 1 course unit

1 course unit

#### MAT 470/Topics in Mathematics 1 course unit (occasionally) variable course units MAT 492/Guided Study in Mathematics II (every semester) This course allows student to study advanced mathematical topics under the supervision of a faculty member. MAT 493/Independent Research II in Mathematics variable course units (every semester) *Prerequisite:* By invitation only Student will study and or do research independently in an appropriate area. A department member will be assigned to advise and direct the student. MAT 494/Independent Study in Mathematics II variable course units (every semester) The course allows students to study advanced mathematical topics independently under the supervision of a faculty member.

#### MAT 498/Capstone

(every semester) Prerequisite: Senior standing Intensive study of advanced topics in mathematics. Students will write and present an expository paper in mathematics.